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# Adsorption of Lead, manganese, and copper onto biochar in landfill leachate: implication of non-linear regression analysis



Ali Daryabeigi Zand\* and Maryam Rabiee Abyaneh

# **Abstract**

The feasibility of using wood-derived biochar (BC) to remove Pb, Mn, and Cu from landfill leachate was investigated and modeled in this study. BC was produced under the pyrolytic temperature of 740 °C. The effect of contact time, BC dosage and particle size on adsorption of the heavy metals onto BC was examined. BC was used in two forms i.e., pulverized (PWB) and crushed (CWB) to evaluate the effect of BC particle size on adsorption characteristics. The kinetics of Pb, Mn, and Cu adsorption onto PWB and CWB were assessed using the pseudo second-order and Elovich models, where both applied models could well describe the adsorption kinetics. Removal efficiencies of the heavy metals were increases by 1.2, 1.4, and 1.6 times, respectively, for Pb, Mn, and Cu, when PWB content of the leachate increased from 0.5 to 5 g L<sup>-1</sup>. Equilibrium adsorption capacity of the heavy metals onto BC in leachate system was evaluated using the Langmuir, non-linearized Freundlich, linearized Freundlich, and Temkin isotherms and found to have the following order for PWB: Non-linearized Freundlich > Temkin > Langmuir > Linearized Freundlich. The Langmuir and linearized Freundlich models could not adequately represent adsorption of the heavy metals onto BC, especially for CWB. The highest removal of 88% was obtained for Pb, while the greatest adsorption intensity was found to be 1.58 mg g<sup>-1</sup> for Mn. Using the non-linearized Freundlich isotherm significantly reduced adsorption prediction error. The adsorption affinity of PWB for Pb, Mn, and Cu was greater than that of CWB in all treatments. Wood-derived BC is suggested to be used for the removal of heavy metals from landfill leachate as an economical adsorbent.

**Keywords:** Adsorption, Biochar, Landfill leachate, Heavy metals, Linearization error

# Introduction

Landfill leachate may contain a wide range of contaminants at levels enough to raise serious environmental and human health concerns. The majority of published research has focused on removal of ammonia and organic fraction of landfill leachates, such as using biological reactors [1], oxidation processes [2] and membrane separation [3]. Concentrations of heavy metals in fresh landfill leachate, characterized by lower pH, are usually higher than those in aged leachate [4]. Adsorption of heavy metals on carbonaceous materials has received considerable attention to remove toxic metals from contaminated aqueous

solutions. Salam investigated the removal of heavy metals from synthetic aqueous solution by adsorption onto carbon nanotubes through a set of batch experiments which showed effective removal of heavy metals [5]. Activated carbon (AC) is a well-known strong adsorbent which has been employed to remove heavy metals from different media principally because of its large surface area and high porosity [6–8]. Palm shell AC was successfully used to remove Cu from aqueous solution [9]; but high production expenses of AC may limit its use as adsorbent [10]. Application of economical alternatives to AC has therefore drawn remarkable attention in recent years. For instance, in a study by Soco and Kalembkiewicz, coal fly ash was successfully used for the removal of nickel and copper from a synthetically contaminated aqueous solution [11].

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Adsorption process rate is usually studied using kinetic models, while the variation in the amount of sorbate adsorbed by different doses of adsorbent is evaluated by isotherm models, which is critical in optimizing the use of adsorbents. Various models have been proposed to study adsorption of heavy metals onto carbonous materials in aqueous solutions [12-14]. The adsorption kinetics of Pb and Zn onto carbon nanotubes in aqueous solutions were described well using pseudo-second-order and Elovich models. Lagergren pseudo-first-order model was not able to predict adsorption kinetics of the metals as precise as pseudo-second-order and Elovich models [5]. The applicability of the pseudo-second-order and Elovich models to predict adsorption kinetics of heavy metals in contaminated aqueous solutions has been reported in the literature [15-17]. Temkin isotherm model assumes that the heat of adsorption of all the molecules in layer declines as adsorbent surface coverage increases due to adsorbateadsorbate repulsions. Fall in the heat of adsorption is considered to be linear for Temkin isotherm rather than logarithmic. Adsorption of adsorbate onto adsorbent is also characterized by a unisonous distribution of binding energies up to ca. maximum binding energy [14]. Adsorption of chlorophenoxyacetic acid herbicides from water onto orange peel AC was successfully described by Temkin isotherm model [18]. Moreover, the Temkin model could satisfactory predict adsorption of Cr(VI) onto AC, though higher R<sup>2</sup> values were found using the Freundlich and Langmuir equations [19]. Freundlich and Langmuir equations are the most well-known models for describing adsorption isotherm [20]; but applying non-linearized form of the Freundlich model in adsorption studies has been scant. Isotherm and kinetic models are often applied in linear form, though linearization of the original model might violate the theories and assumptions behind the development of a given model. That means when model parameters are estimated based on linear transformation it would not necessarily yield the best fitting parameters for the nonlinear original model [21]. Error analysis for the kinetic and isotherm models, which has rarely been studied in adsorption of heavy metals onto biochar (BC) in landfill leachate, was also investigated in this paper.

Recently, use of BC has attracted considerable attention [22]. de Caprariis et al. employed BC to remove total organic carbon from wastewater, and a very high sorption capacity of BC (840 mg g<sup>-1</sup>) was achieved [23]. In another study, BC derived from sewage sludge eliminated Cr from water significantly by 89%, whereas As removal did not exceed 53% [24]. Many studies have focused on the immobilization and mitigation of contaminants, respectively, in soil and effluents [25, 26]; however, removal of heavy metals from landfill leachate by BC has rarely been investigated. This research aimed to investigate the adsorption of Pb, Mn and Cu onto wood-derived BC in fresh

landfill leachate. We specifically studied: (i) effect of contact time, BC dosage and particle size on adsorption of heavy metals onto BC; (ii) adsorption kinetics of the heavy metals onto BC in landfill leachate using pseudo second-order and Elovich models; and (iii) modeling of adsorption of the heavy metals onto BC in landfill leachate using Freundlich (linearized and non-linearized), Langmuir and Temkin isotherms.

#### Materials and methods

# Site description and leachate sampling and analysis

Kahrizak landfill which is also known as Aradkooh waste disposal and processing complex is main disposal site of the capital city of Tehran, located at a 25 km distance from the southern part of the capital city of Tehran having longitude of 51°19′18" E and latitude of 35°27′52" N. More than 8 kt of wastes are transferred daily to the landfill site. Household hazardous wastes are buried together with general wastes. Generated leachate at Kahrizak landfill is a serious environmental and health threat. High clay content and therefore low permeability of the land around the landfill caused infiltration of the landfill leachate to be minimal. Therefore, freshly generated leachate at Kahrizak landfill, which is now estimated to be about 637 m<sup>3</sup> d<sup>-1</sup> [27], flows gravitationally towards the low land next to the burial site creating a leachate lake with a depth of ca. 10 m, with seasonal variations. In this study, the leachate samples were directly collected from the generated leachate stream at the bottom of the waste discharge place at Kahrizak landfill and used for the adsorption experiments. Overflow of the fresh leachate from newly-filled trenches was directly collected in four 10-L plastic containers. Collected leachate can be classified as relatively fresh leachate based on the low pH values (5.11). Leachate samples were immediately transported to the laboratory. Samples were kept refrigerated at 4°C without exposure to the ambient air for not more than 3 days before conducting relevant analysis to prevent potential chemical and biological changes.

Leachate samples characterized according to the Standard Methods for the Examination of Water and Wastewater [28]. Raw samples were filtered using Whatman Paper Filter No. 1 (pore size: 11 µm) prior to acid digestion in order to remove particles larger than 11 µm. Leachate samples were digested with nitric acid, then the digestate passed through MILEXHA 0.45 µm diameter filter followed by the US EPA 3005A method [29]. Partially filtered samples containing suspended particles (up to 11 µm) were analyzed for heavy metal content to imitate close to real conditions, as when landfill leachate is analyzed to control compliance with permissible limits. Samples were digested in triplicate and analyzed for the concentrations of Cd in the final solution using an atomic absorption spectrometer (*Perkin Elmer 700*). Organic load of the leachate produced at this landfill is markedly higher than that of leachate generated in many other countries [13, 30]; due to the high content of organics such as food wastes. Received municipal solid wastes at Kahrizak landfill is characterized by putrifiable fraction of ca. 68% and moisture content of 65-70% that significantly contribute to high organic load of produced leachate. Elevated ratio of biological oxygen demand (BOD)/chemical oxygen demand (COD) for landfill leachate as observed in this study indicates the high concentration of biodegradable organic compounds in leachate, and hence a good potential to be biologically degraded. Some characteristics of the leachate are as follow: COD (71,245 mg L<sup>-1</sup>); BOD (32,187 mg L<sup>-1</sup>); BOD/ COD (0.45); Total suspended solids (19,800 mg  $L^{-1}$ ); Total dissolved solids  $(11,480 \text{ mg L}^{-1})$ ; NO<sub>3</sub>-N (70 mg) $L^{-1}$ ),  $SO_4$  (1698 mg  $L^{-1}$ ); electrical conductivity (28.86) mS cm<sup>-1</sup>); pH (5.11) and Pb (1.90 mg L<sup>-1</sup>), Mn (7.78  $mg L^{-1}$ ) and Cu (2.52  $mg L^{-1}$ ) [28].

## **BC** preparation

Fresh urban yard trimmings with no pollution background was initially chopped into wood chips of 5-10 cm length and then oven-dried for 48 h. Yard trimmings can be found abundantly in most places and often used for composting or find their way into urban waste stream. Dried wood chips were placed in open crucibles, then weighted, and covered thoroughly with aluminum foil in order to provide an oxygen-limited environment. BC derived from the wood chips was produced under the pyrolytic temperature of up to 740 °C with a temperature gradient of ca. 10 °C min<sup>-1</sup> until the desired temperature of 740 ± 5 °C was reached in the muffle furnace under the atmospheric pressure with residence time of 42 min. At the end, samples were kept in the furnace overnight to let them cool down to the room temperature. The produced BC chips were air-dried over a week, ground using a ceramic mortar and pestle and sieved to gain homogenous crushed wood-derived BC (CWB), with the particle size of 1 to 2 mm. Moreover, some BC chips were further ground and sieved to 63-75 µm diameter to yield fine-graded BC to be used as pulverized wood-derived BC (PWB) in the adsorption experiments. Elemental composition of the produced BC was as follow (dry basis): C (81.5%), O (11.2%), H (3.3%), N (0.5%), S (0.1%) and ash (3.4%). The produced BC had particle density of 1.5 g cm<sup>-3</sup>. PWB and CWB had bulk densities of 0.93 and 0.69 g cm<sup>-3</sup>, respectively. The pH of the BC (9.1) was determined following the method of Singh et al. [31]. BET surface area was measured using a Brunauer-Emmett-Teller Surface Area & Porosity Analyzer (NOVA 4200e) by nitrogen gas sorption analysis at 77 K. Samples were vacuum degassed prior to analysis, at 300 °C for 5 to 15 h, based on the required time to reach a stable surface area measurement [32].

BET surface area of the PWB and CWB were determined to be 335 and 281  $\text{m}^2\ \text{g}^{-1}$ , respectively.

#### Adsorption experiment

The adsorption process of Pb, Mn and Cu was conducted under the adjusted pH of 5.1 in order to eliminate the possibility of formation of metal hydroxide precipitates. Solutions were initially adjusted for the desired pH, and then the BC was added. Values of pH were measured during the experiments once (for experiments below 600 min) or twice (for experiments longer than 600 min) for probable pH adjustment. Precipitation of heavy metal hydroxides between the pH values of 6.5-7 was reported for heavy metals [33]. Adsorption of heavy metals onto PWB and CWB was carried out versus time at specified intervals up to 24 h. Actual concentrations of Pb, Mn and Cu ions in leachate samples were considered as the initial concentration, to simulate real conditions. Each adsorption experiment was conducted in triplicate and the mean values were reported. The percentage removal of heavy metals in the solution was calculated using the following equation

$$R\left(\%\right) = \frac{C_0 - C_e}{C_0} \times 100\tag{1}$$

where, C<sub>0</sub> and C<sub>e</sub> are, respectively, the initial and final concentrations of Pb, Mn and Cu in leachate samples (mg L<sup>-1</sup>). Kinetic solutions were stirred on a shaker at constant rate of 120 rpm at room temperature of 24 ± 2°C to provide effective interaction of sorbate with sorbent material. At the end of the specified agitation period, obtained mixtures were centrifuged for 15 min at 6000 rpm to separate liquid and solid phases, filtered by Whatman Paper Filter No. 1 (11 µm pore size) and the filtrates were then analyzed for the heavy metal concentrations. The adsorption isotherms were studied in actual leachate system for Pb, Mn and Cu. Certain quantities of PWB and CWB (0.05 to 5g) were separately weighted and added to a 100 mL fresh landfill leachate at initial pH of 5.1. The pseudo first-order, pseudo second-order and Elovich models were used to study the kinetics of adsorption of Pb, Mn and Cu onto BC in landfill leachate and the Langmuir, non-linearized and linearized Freundlich, and Temkin isotherm models were applied to fit the measured data.

### Error analysis for the kinetic and isotherm models

Non-linear regression as a more general technique to estimate parameters of adsorption models can be used even if the model cannot be linearized. However, isotherm and kinetic models are mainly applied in linear form because less difficult calculations are required to find model parameters. It should be noticed that modifying and linearization

of the original model might violate the theories and assumptions behind the development of a given model that means when parameters are estimated based on linear transformation of a given model it does not necessarily yield best fitting parameters for the nonlinear original model [34]. Error structure of experimental data has been found to be altered when adsorption isotherms transformed into linearized forms. Non-linear regression usually minimizes the error distribution between the experimental and predicted data, unlike linear regression [35]. Therefore, linear determination coefficient (R2) should be used to measure the matching degree between experimental and predicted data when linear form of a given adsorption kinetic or isotherm model is applied. Beside linear R<sup>2</sup>, the applicability of the applied models can also be verified through error analysis techniques such as sum of error squares (SSE). The SSE is said to be among the widespread used error functions. It can be written as:

$$SSE (\%) = \frac{\sqrt{\sum \left(q_{e(Exp)} - q_{e(Cal)}\right)^2}}{N}$$
 (2)

where,  $q_{\rm e(Exp)}$  is the adsorption capacity at equilibrium condition obtained from adsorption experiments,  $q_{\rm e(Cal)}$  is the calculated value of adsorption capacity at equilibrium state, and N is the number of data points [36].

# **Results and discussion**

# Effect of contact time on the adsorption of Pb, Mn, and cu onto BC in the leachate

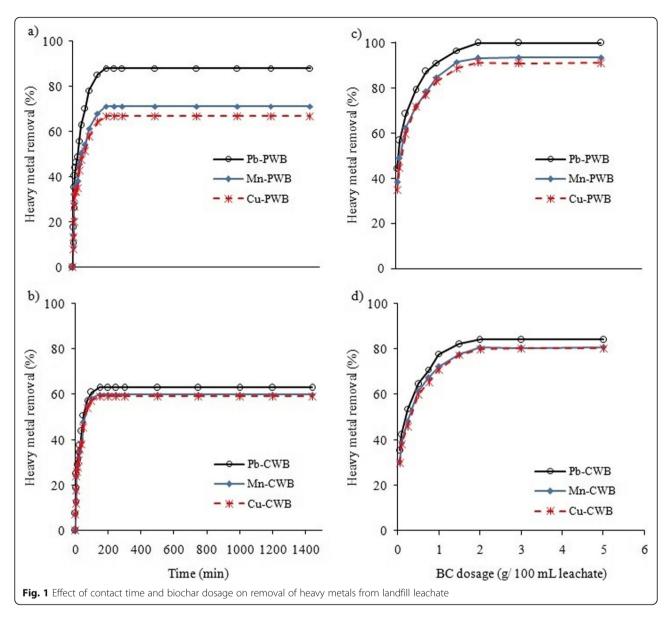
The effect of contact time on the adsorption of Pb, Mn, and Cu in landfill leachate is shown in Fig. 1a and b. The adsorbent dosage was fixed at 1 g 100 mL<sup>-1</sup> (10 g L<sup>-1</sup>) and the pH value of the fresh leachate was 5.1. The removal efficiency of the heavy metals experienced a drastic initial increase followed by a gradual rise to reach a plateau, which indicates equilibrium condition. Instant adsorption rate of heavy metals onto BC gradually declined to zero with the equilibrium point of adsorption lay between 150 and 200 and 100-150 min for, respectively, PWB and CWB, suggesting that the contact time of 200 and 150 min is sufficient to establish dynamic balance. The importance of contact time to provide sufficient contact between adsorbates and adsorbent surface has been emphasized by several authors [35, 37]. It can be inferred from Fig. 1a and b that the removal of Pb, Mn, and Cu was greater when PWB was used as adsorbent, compared to CWB. Moreover, longer period of contact time was required for the equilibrium state to be established when BC with smaller particle size, i.e., PWB was used, implying slower occupation of adsorption sites on the surface of PWB due to the greater specific surface provided by PWB relative to CWB. The highest removal efficiency of 88% by PWB was obtained for Pb.

As reaction time prolonged, repulsive forces between the metal ions adsorbed to BC and those in the aqueous phase might be increased. In addition, unoccupied adsorption sites and therefore adsorption efficiency will be quickly declined until the establishment of dynamic balance in the system. The same observation was found for Ni uptake from aqueous solution by AC derived from sugar bagasse [37]. From the adsorption diffusion viewpoint, two distinct adsorption stages could be distinguished for the uptake of Pb, Mn, and Cu onto BC in landfill leachate; surface diffusion during which the mass transfer is rapid and physical processes control the adsorption, followed by intra-particle diffusion that is characterized by slow adsorption. Greater adsorption efficiency for heavy metals was observed for all the applied dosages of BC at initial stages of the experiment, that may be attributed to the higher availability of adsorption sites on BC surface which are rapidly occupied by the solutes in the leachate. When equilibrium is reached mass transfer from the leachate to the surface of BC was significantly restricted (Fig. 1a and b), which is consistent with those reported in the literature [13].

# Effect of BC dosage on the adsorption of heavy metals in landfill leachate

BC dosage varied from 0.05 to  $5 g 100 mL^{-1}$  (0.5 to 50 gL<sup>-1</sup>) at initial pH of 5.1, with the reaction times of 200 and 150 min, respectively, for PWB and CWB. Results indicated that the removal efficiency of the heavy metals was significantly raised by 1.2, 1.4, and 1.6 times, respectively, for Pb, Mn, and Cu, when PWB content of the leachate increased from 0.5 to 5 g L<sup>-1</sup>. Obtained results are consistent with the literature, where removal of Ni from aqueous phase increased by AC dosage [37]. The removal efficiency of Pb, Mn, and Cu did not change significantly as BC content exceeded 2 g 100 mL<sup>-1</sup> in leachate. It suggests the optimal dosage of 20 g L<sup>-1</sup> for both PWB and CWB to achieve the highest economical adsorption capacity for the heavy metals. Unsaturated adsorption sites may increase as BC dosage exceeds the optimum amount. The highest removal efficiency was obtained for Pb followed by Mn and Cu due to addition of PWB (Fig. 1c) and CWB (Fig. 1d).

Removal efficiency of Mn and Cu was comparable, with slightly higher elimination for Mn. Amount of Pb, Mn, and Cu adsorbed to each gram of BC reduced with rising adsorbent dosage, likely due to the availability of more adsorption sites on the surface of both PWB and CWB. Optimum AC dosage of 7 g 100 mL<sup>-1</sup> was found to effectively adsorb COD and NH<sub>3</sub> from landfill leachate [13], which is markedly higher than the optimum dosage of BC obtained in this study. It might be attributed to the higher



levels of COD and NH<sub>3</sub> in leachate compared to those of heavy metals in this study. BC dosage may also induce pH variation, which in turn affects adsorption of adsorbates in aqueous systems by changing the adsorbent surface charge and degree of ionization of adsorbates. Addition of high levels of BC to fresh leachate may increase pH and promote the formation of metal hydroxides. However, adverse effect of low pH on adsorption of Ni onto AC has been reported due to competence with hydrogen ions [38]. The influence of pH on adsorption of heavy metals on various adsorbents has been well documented [14].

### Adsorption kinetics

Batch kinetic experiments were carried out for the adsorption of Pb, Mn, and Cu onto PWB and CWB in landfill leachate. Lagergren pseudo-first-order model is

also one of the most widely used equations to describe adsorption kinetics. However, pseudo-first-order model was not able to well describe adsorption kinetics of heavy metals onto carbonous materials in some studies [5]. In addition, preliminary calculations conducted in this research indicated non-sufficient description of adsorption kinetics of Pb, Mn and Cu onto PWB and CWB in the landfill leachate (data not shown). Therefore, the kinetics for adsorption of heavy metals onto BC was simulated using two kinetic models: pseudo second-order and Elovich kinetic models. The experimental effectiveness is controlled by the adsorption kinetics. Adsorption kinetic models are typically used to investigate the adsorption mechanism and the potential rate of the processes such as mass transfer and chemical reactions [13].

### Pseudo second-order kinetic model

The non-linear form of pseudo second-order model is represented as follow:

$$q_t = \frac{k_{2p}q_e^2 t}{1 + k_{2p}q_e t} \tag{3}$$

where  $k_{2p}$  is the second-order adsorption constant (g mg<sup>-1</sup> min<sup>-1</sup>),  $q_e$  is the amount of heavy metals adsorbed onto BC when dynamic balance researched (mg g<sup>-1</sup>), and  $q_t$  is the amount of adsorbate adsorbed onto BC at any time, t. In order to gain the linear form of the pseudo second-order kinetic model the following equation should be solved through integration:

$$\frac{\mathrm{d}q_{\mathrm{t}}}{\mathrm{d}t} = k_{\mathrm{2p}}(q_{\mathrm{e}} - q_{\mathrm{t}})^{2} \tag{4}$$

If the boundary conditions of  $q_t = 0$  to  $q_t = q_t$  and t = 0 to t = t is applied, the model can be written as follows:

$$\frac{t}{q_{\rm t}} = \frac{1}{k_{\rm 2p} \, q_{\rm e}^{\,2}} + \frac{1}{q_{\rm e}} t \tag{5}$$

Plots of  $t/q_t$  versus t for adsorption of Pb onto PWB and CWB are illustrated in Fig. 2. Similar graphs could be constructed using the obtained data for Mn and Cu, with the same trend as Pb. Figure 2a and b clearly illustrates higher adsorption capacity of PWB compared to CWB for the heavy metals. The pseudo second-order kinetic constants and the theoretical  $q_e$  values using the pseudo second-order expression are given in Table 1 for all the studied metals. Very high values of  $\mathbb{R}^2$  ( $\geq$  0.999) were found for the pseudo second-order kinetic model in all applied levels of PWB and CWB indicating an

excellent linearity. Results showed an excellent agreement between the experimental data and the calculated adsorption capacity by the pseudo second-order kinetic model which is consistent with the literature, where heavy metals in an aqueous solution were removed by carbon nanotubes [5]. Error analysis indicated that deviation occurred by application of the pseudo secondorder kinetic model is very small for all levels of BC, regardless of the BC particle size. This supports the chemisorptions theory behind the pseudo second-order kinetic model for the heavy metals/BC system; however, evaluation of variation of adsorption energy using appropriate isotherms such as Temkin model could provide deeper insight into the nature of metal adsorption onto BC. It can be inferred from Table 1 that the adsorption equilibrium rate for the studied heavy metals, regardless of the BC size, has the following order: Pb > Cu > Mn. The applicability of pseudo second-order model to fit the experimental kinetics data was also reported for adsorption of heavy metals onto sewage sludge [24]. Predicted adsorption capacity decreased by increasing dosage of PWB and CWB. The adsorption process is mainly a surface phenomenon and increase in adsorption sites on the surface of an adsorbent at a constant adsorbate level could result in alleviated adsorption intensity.

# Elovich kinetic model

The Elovich adsorption kinetic equation which was initially developed to describe chemisorption kinetics of gas onto solids [39], has recently gained increasing attention to describe kinetics of adsorption of adsorbates in aqueous phase onto adsorbents. The Elovich kinetic model is expressed as follows:

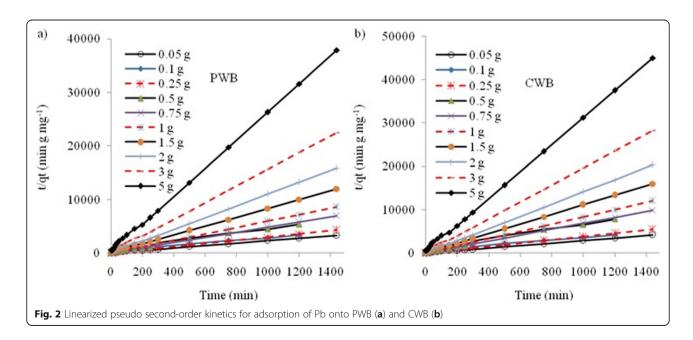


Table 1 Kinetic parameters of the pseudo second-order model for adsorption of heavy metals onto BC in landfill leachate

Adsorbate	BC dosage	Pseudo secor	nd-order kineti	c for PWB		Pseudo second-order kinetic for CWB			
		$\frac{q_{e(cal.)}}{(mg g^{-1})}$	k <sub>2p</sub>	R <sup>2</sup>	SSE	$\frac{q_{e(cal.)}}{(mg g^{-1})}$	k <sub>2p</sub>	R <sup>2</sup>	SSE
Pb	0.05	0.45	0.12	0.999	0.000	0.36	0.15	0.999	0.000
	0.1	0.44	0.12	0.999	0.000	0.35	0.15	0.999	0.000
	0.25	0.34	0.15	0.999	0.000	0.27	0.20	0.999	0.000
	0.5	0.27	0.19	0.999	0.000	0.19	0.28	0.999	0.000
	0.75	0.21	0.24	0.999	0.000	0.15	0.36	0.999	0.000
	1	0.17	0.31	0.999	0.000	0.12	0.47	0.999	0.000
	1.5	0.12	0.43	0.999	0.000	0.09	0.63	0.999	0.000
	2	0.09	0.56	0.999	0.000	0.07	0.79	0.999	0.000
	3	0.07	0.81	0.999	0.000	0.05	1.10	0.999	0.000
	5	0.04	1.39	0.999	0.000	0.03	1.75	0.999	0.000
Mn	0.05	1.62	0.03	0.999	0.001	1.40	0.04	0.999	0.001
	0.1	1.54	0.03	0.999	0.000	1.40	0.04	0.999	0.001
	0.25	1.10	0.05	0.999	0.000	0.97	0.06	0.999	0.000
	0.5	0.85	0.06	0.999	0.000	0.73	0.07	0.999	0.000
	0.75	0.69	0.07	0.999	0.000	0.58	0.09	0.999	0.000
	1	0.56	0.09	0.999	0.000	0.47	0.12	0.999	0.000
	1.5	0.43	0.12	0.999	0.000	0.36	0.16	0.999	0.000
	2	0.34	0.15	0.999	0.000	0.28	0.20	0.999	0.000
	3	0.24	0.22	0.999	0.000	0.20	0.28	0.999	0.000
	5	0.15	0.35	0.999	0.000	0.13	0.45	0.999	0.000
Cu	0.05	0.40	0.13	0.999	0.000	0.46	0.11	0.999	0.000
	0.1	0.39	0.13	0.999	0.000	0.43	0.12	0.999	0.000
	0.25	0.33	0.16	0.999	0.000	0.32	0.17	0.999	0.000
	0.5	0.26	0.20	0.999	0.000	0.24	0.23	0.999	0.000
	0.75	0.22	0.24	0.999	0.000	0.18	0.29	0.999	0.000
	1	0.17	0.29	0.999	0.000	0.16	0.37	0.999	0.000
	1.5	0.13	0.38	0.999	0.000	0.12	0.49	0.999	0.000
	2	0.11	0.49	0.999	0.000	0.09	0.62	0.999	0.000
	3	0.08	0.70	0.999	0.000	0.07	0.87	0.999	0.000
	5	0.05	1.09	0.999	0.000	0.04	1.38	0.999	0.000

$$\frac{\mathrm{d}q_{\mathrm{t}}}{\mathrm{d}t} = \alpha \ \exp\left(-\beta \ q_{\mathrm{t}}\right) \tag{6}$$

where  $\alpha$  is the initial adsorption rate (mg g<sup>-1</sup> min<sup>-1</sup>) and  $\beta$  is defined as desorption constant (g mg<sup>-1</sup>) during any experiment [36]. Elovich differential equation can be solved assuming  $\alpha$   $\beta_t >> 1$  and by applying the boundary conditions of  $q_t = 0$  at t = 0 and  $q_t = q_t$  at t = t [39]. Therefore, the linear form of the Elovich equation can be presented as follows:

$$q_{\rm t} = \frac{1}{\beta} \ln(\alpha \beta) + \frac{1}{\beta} \ln t \tag{7}$$

In order to study the adsorption kinetics using Elovich model a straight line of  $q_t$  versus  $\ln t$  should be plotted

to be able to calculate the model constants of  $\alpha$  and  $\beta$  from the slope and the intercept of the plot. For instance, Pb adsorption capacity of BC predicted by the Elovich kinetic model is shown in Fig. 3. Parameters of the Elovich kinetic model for adsorption of Pb, Mn and Cu onto PWB and CWB are presented in Table 2. Pretty high  $R^2$  and low SSE values obtained for the Elovich kinetic model suggesting that adsorption kinetics of the heavy metals onto BC in landfill leachate can be adequately represented by the Elovich kinetic model. However, higher values of  $R^2$  and lower values of SSE were found for the pseudo second-order kinetic model compared to the Elovich kinetic expression in this study. Comparison of the kinetic data obtained in this study

suggests pseudo second-order kinetic expression is the optimum kinetic expression to represent adsorption of Pb, Mn, and Cu onto BC in landfill leachate.

# Modeling of adsorption isotherms

The equilibrium data were modeled using the Langmuir, non-linearized Freundlich, linearized Freundlich and Temkin isotherms in this study to predict adsorption capacity of PWB and CWB for heavy metals in landfill leachate. Experimental data versus the predicted adsorption of Pb, Mn and Cu onto BC in the leachate using different adsorption isotherms are shown in Fig. 4. Experimental results indicated that Pb could be adsorbed on BC to a higher degree than Mn and Cu. Adsorption of Mn on BC was comparable with that of Cu with slightly higher adsorption for Mn.

# Langmuir isotherm

The Langmuir model which is an empirical isotherm assumes uniform energies of adsorption onto the adsorbent surface with no interaction between adsorbate molecules on adjacent sites. All adsorption is also assumed to occur through the same mechanism to form a layer with a thickness of one molecule on solid surface [25]. Once a site is occupied, no further adsorption can proceed at that site based on the Langmuir isotherm representing the surface saturation condition. Langmuir isotherm has been extensively used to evaluate adsorption capacity of a wide range of contaminants such as heavy metals, organic pollutants and dyes [12]. Langmuir model describes a

homogeneous adsorption assuming that all the adsorption sites on the surface of a given adsorbent have equal solute affinity. It is also assumed that adsorption of solute at one site does not affect the adsorption at an adjacent site [40]. Therefore, the maximum adsorption capacity obtained by using the Langmuir isotherm is based on complete monolayer coverage of the surface of adsorbent. All adsorption is assumed to occur through the same mechanism. The non-linear expression of Langmuir isotherm model can be illustrated as follows:

$$q_e = \frac{q_m b C_e}{1 + b C_o} \tag{8}$$

where, b is adsorption equilibrium constant (L mg<sup>-1</sup>) which is related to the apparent energy of adsorption, and  $q_{\rm m}$  is the quantity of adsorbate required to form a single monolayer on unit mass of a given adsorbent (mg g<sup>-1</sup>).

Values of the constants for different types of linearized Langmuir isotherm are presented in Table 3 for the adsorption of Pb, Mn and Cu onto BC. The applied linearized forms of Langmuir isotherm equation is among the most frequently used linearized forms in the literature [41]. Langmuir isotherm can be further analyzed and the favorable nature of adsorption of adsorbate onto adsorbent can be expressed through determination of the separation factor,  $R_{\rm L}$ , which is a dimensionless equilibrium parameter defined by the following equation:

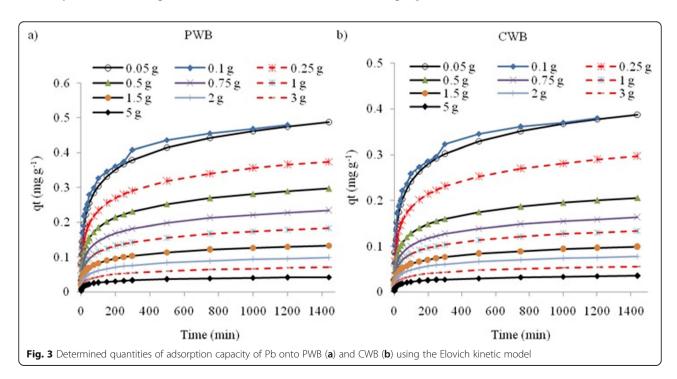


Table 2 Kinetic parameters of the Elovich model for adsorption of heavy metals onto BC in landfill leachate

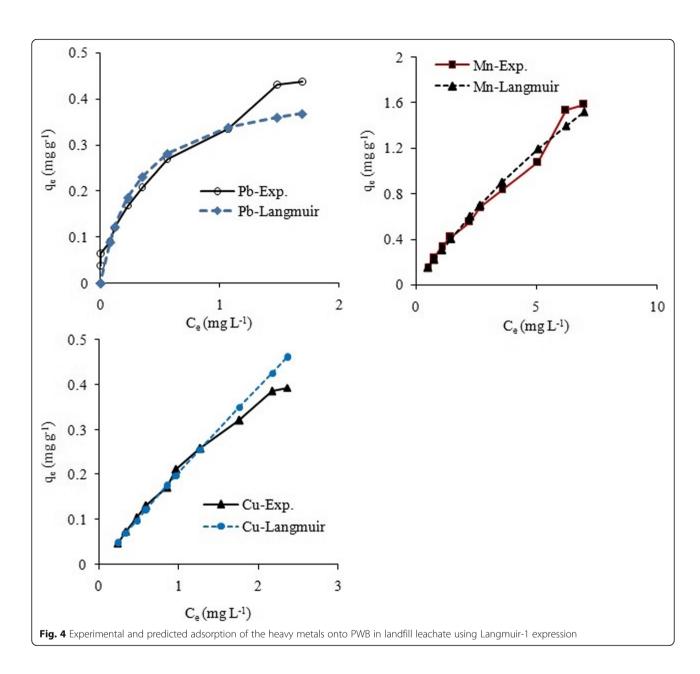
Adsorbate	Adsorbent dosage	$q_{e(cal.)} (mg g^{-1})$	Elovich kinetics for PWB					Elovich kinetics for CWB			
			β	α	$R^2$	SSE	$q_{e(cal.)}$ (mg $g^{-1}$ )	β	α	$R^2$	SSE
Pb	0.05	0.49	14.5	0.056	0.953	0.002	0.39	18.2	0.044	0.955	0.001
	0.1	0.48	14.7	0.055	0.952	0.002	0.38	18.5	0.043	0.956	0.001
	0.25	0.37	18.9	0.043	0.948	0.002	0.30	23.8	0.034	0.955	0.001
	0.5	0.30	23.8	0.034	0.948	0.001	0.21	34.5	0.024	0.955	0.000
	0.75	0.23	30.3	0.027	0.949	0.001	0.16	43.5	0.019	0.955	0.000
	1	0.18	38.5	0.021	0.937	0.000	0.13	52.6	0.015	0.951	0.000
	1.5	0.13	52.6	0.015	0.937	0.000	0.10	71.4	0.011	0.951	0.000
	2	0.10	71.4	0.011	0.937	0.000	0.08	90.9	0.009	0.951	0.000
	3	0.07	100.0	0.008	0.939	0.000	0.06	125.0	0.006	0.951	0.000
	5	0.04	166.7	0.005	0.935	0.000	0.04	200.0	0.004	0.952	0.000
Mn	0.05	1.76	4.0	0.201	0.952	0.032	1.55	4.6	0.176	0.956	0.028
	0.1	1.71	4.1	0.195	0.952	0.031	1.53	4.6	0.174	0.956	0.026
	0.25	1.20	5.9	0.137	0.948	0.016	1.07	6.6	0.121	0.955	0.013
	0.5	0.84	8.6	0.107	0.948	0.000	0.81	8.8	0.092	0.955	0.008
	0.75	0.76	9.3	0.086	0.948	0.006	0.63	11.1	0.072	0.954	0.005
	1	0.61	11.5	0.07	0.937	0.004	0.52	13.6	0.059	0.95	0.003
	1.5	0.47	15.2	0.053	0.937	0.002	0.38	18.9	0.045	0.95	0.001
	2	0.37	18.9	0.043	0.937	0.002	0.31	22.8	0.035	0.95	0.001
	3	0.26	27.0	0.03	0.936	0.001	0.23	31.3	0.026	0.95	0.001
	5	0.16	43.5	0.019	0.936	0.000	0.14	50.0	0.016	0.95	0.000
Cu	0.05	0.45	15.9	0.051	0.952	0.003	0.51	13.9	0.058	0.957	0.003
	0.1	0.44	16.1	0.050	0.952	0.003	0.47	15.2	0.053	0.957	0.002
	0.25	0.35	20.0	0.041	0.948	0.001	0.35	20.0	0.041	0.955	0.001
	0.5	0.28	25.0	0.032	0.948	0.001	0.26	27.0	0.030	0.955	0.001
	0.75	0.23	30.3	0.027	0.948	0.000	0.20	35.8	0.023	0.954	0.000
	1	0.19	37.0	0.022	0.937	0.000	0.17	41.7	0.019	0.955	0.000
	1.5	0.14	50.0	0.016	0.937	0.000	0.13	55.6	0.014	0.955	0.000
	2	0.11	62.5	0.013	0.937	0.000	0.10	71.4	0.011	0.949	0.000
	3	0.08	90.9	0.009	0.936	0.000	0.07	100.0	0.008	0.949	0.000
	5	0.05	142.9	0.006	0.937	0.000	0.04	166.7	0.005	0.948	0.000

$$R_L = \frac{1}{1 + bC_0} \tag{9}$$

where b is the Langmuir model constant related to the free energy of adsorption (L mg $^{-1}$ ). The  $R_{\rm L}$  indicates the shape of the isotherm. Values of  $0 < R_{\rm L} < 1$  indicates favorable adsorption, whereas  $R_{\rm L} > 1$  represents an unfavorable adsorption. In addition,  $R_{\rm L} = 0$  represents irreversible adsorption, while the adsorption is linear if  $R_{\rm L} = 1$  [21, 42]. The dimensionless  $R_{\rm L}$  values calculated for adsorption of the heavy metals onto PWB were between zero to one showing favorable adsorption, while

the corresponding values for CWB were greater than 1 indicating an unfavorable adsorption (Table 3).

The values of  $R^2$  and  $R_L$  obtained from Langmuir expression indicate positive evidence that the adsorption of Pb, Mn, and Cu onto PWB follows the Langmuir isotherm. The fit of the measured data to the Langmuir model reveals the possibility of sorption of the heavy metals onto PWB through chemisorptions [43]. Negative values obtained for maximum adsorption capacity of CWB reveals that adsorption of Pb, Mn and Cu onto CWB in the leachate does not follow Langmuir isotherm. In another study, negative values for adsorption capacity of dyes onto AC was obtained [35], which is practically and experimentally impossible. The highest



**Table 3** Parameters of the Langmuir isotherm for adsorption of Pb, Mn and Cu onto BC in landfill leachate

Langmuir	Pb		Mn		Cu		
isotherm- type 1	PWB	CWB	PWB	CWB	PWB	CWB	
$q_m (mg g^{-1})$	0.44	-0.22	5.60	-0.65	5.90	-0.21	
b ( $L mg^{-1}$ )	3.22	-0.46	0.05	-0.12	0.04	-0.37	
$R^2$	0.985	0.965	0.993	0.944	0.994	0.944	
$R_L$	0.14	8.86	0.70	23.05	0.92	18.28	
SSE	0.016	0.364	0.045	9.593	0.008	0.842	

value of the Langmuir constant *b*, 3.2 L mg<sup>-1</sup>, was obtained for Pb adsorption onto PWB (Table 3) exhibiting greater affinity of Pb for the surface of PWB compared to Mn and Cu in landfill leachate. It seems that the monolayer adsorption capacity of Pb onto PWB provides a better fit to the experimental data compared to Mn and Cu. Experimental results showed that adsorbed amounts of the heavy metals on BC were clearly increased with rising adsorbent dosage. Figure 4 compares the simulated isotherm curves and measured data for adsorption of Pb, Mn and Cu onto BC based on Langmuir expression. Results indicated that Langmuir isotherm is unable to describe the equilibrium data perfectly in most cases.

### Linearized and non-linearized Freundlich isotherms

The Freundlich isotherm has been widely applied to characterize the adsorption of organic and inorganic pollutants using various adsorbents [44]. Freundlich isotherm constants found through plotting  $\ln q_e$  vs  $\ln C_e$  are given in Table 4. The ratio of the amount of adsorbate adsorbed onto a given mass of adsorbent to the adsorbate concentration in the solution using the Freundlich model is represented by the following equation:

$$q_e = K_F C_e^{\frac{1}{n}} \tag{10}$$

where,  $K_{\rm f}$  is the Freundlich constant representing the relative adsorption intensity of the adsorbent related to the bonding energy, and n is the heterogeneity factor indicating the deviation from linearity of adsorption which is commonly known as Freundlich coefficient. Linearized form of the Freundlich isotherm can be used to evaluate the adsorption data and determine the Freundlich model constants as follows:

$$\ln q_e = \ln K_F + \frac{1}{n} \ln C_e \tag{11}$$

The corresponding coefficients of correlation for Freundlich model were found to be high for adsorption of Pb, Mn, and Cu onto PWB and CWB ( $\geq$  0.99) indicating a good linearity; however, the values of Freundlich coefficient, n, did not fall within the favorable range for CWB. Favorability of the Freundlich isotherm is generally indicated by the magnitude of the exponent n. The values of n ranging from 2 to 10 is stated to represent a good fit, values ranging from 1 to 2 indicates relatively difficult adsorption, and less than 1 shows poor adsorption characteristics [45]. Acceptable adsorption characterized by values of n between 1 and 10 has also been reported in the literature [21, 46]. The highest value of

the Freundlich coefficient was obtained for adsorption of Pb onto PWB (n=2.0) (Table 4). Higher values of  $K_{\rm f}$  were found for adsorption of the heavy metals onto PWB indicating the greater relative adsorption capacity of PWB compared to CWB to eliminate Pb, Mn, and Cu from the landfill leachate. Results show that linearized Freundlich and Langmuir models could not adequately describe adsorption of Pb, Mn, and Cu onto CWB in landfill leachate. In order to find the Freundlich maximum adsorption capacity,  $q_m$ , it is necessary to keep the initial concentration of adsorbate constant and use the variable dosage of adsorbent; that means  $ln\ q_m$  is the extrapolated value of  $ln\ q$  for  $C=C_0$ . Thus, the Freundlich maximum adsorption capacity can be described as follows:

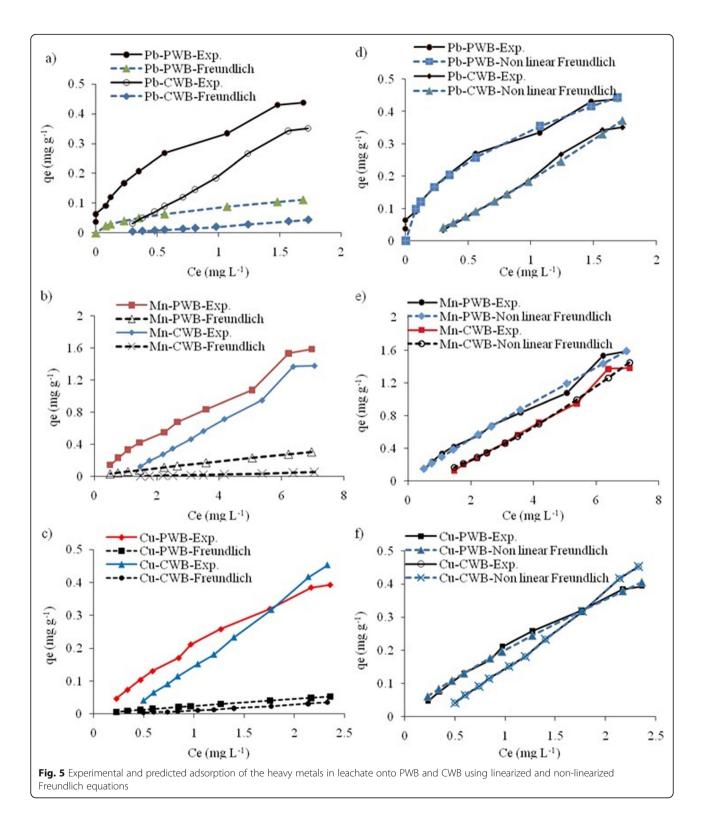
$$q_m = K_F(C_0)^{\frac{1}{n}} \tag{12}$$

where,  $q_m$  is the Freundlich maximum adsorption capacity (mg g<sup>-1</sup>). The calculated maximum adsorption capacity of PWB for Pb, Mn, and Cu using the Freundlich isotherm were greater than the corresponding values for CWB, respectively, by a factor of 2.3, 5.3, and 1.4. Comparing the maximum adsorption capacity produced by application of the Freundlich and Langmuir-1 models reveals that predicted  $q_{max}$  using the Freundlich isotherm is markedly lower than the corresponding values obtained by the Langmuir-1 expression for PWB.

It can be inferred from the Fig. 5a, b and c that the predicted adsorption capacity of PWB and CWB using the linearized Freundlich isotherm is drastically underestimated for Pb, Mn and Cu. Experimental data on adsorption of the heavy metals onto BC in landfill leachate also suggest higher performance of PWB than CWB. Adsorbent particle size may considerably affect removal of target contaminants from aqueous solutions. Higher effectiveness of PWB compared to CWB in sorption of heavy metals in landfill leachate can also be attributed to

Table 4 Linearized and non-linearized Freundlich isotherm constants for adsorption of Pb, Mn and Cu onto BC

Isotherm	Parameters	Pb		Mn		Cu	
		PWB	CWB	PWB	CWB	PWB	CWB
Linearized Freundlich Isotherm	K <sub>F</sub>	0.09	0.02	0.06	0.00	0.02	0.01
	n	1.99	0.74	1.14	0.67	1.11	0.67
	$R^2$	0.994	0.994	0.992	0.990	0.991	0.991
	q <sub>max</sub>	0.12	0.05	0.34	0.06	0.06	0.04
	SSE	0.374	0.312	5.086	5.536	0.446	0.528
Non-linearized Freundlich Isotherm	$K_{F}$	0.34	0.19	0.28	0.91	0.20	0.14
	n	2.03	0.81	1.11	0.72	1.22	0.71
	$R^2$	0.967	0.990	0.988	0.989	0.993	0.998
	q <sub>max</sub>	0.47	0.42	1.75	1.65	0.43	0.53
	SSE	0.0064	0.0012	0.0281	0.0216	0.0009	0.0004



the increased internal surface area with decreasing BC particle size [47]. Smaller particle size provides high capability of adsorption as a result of transfer of heavy metals through shorter pathways inside the adsorbent particle pores [48]. In a previous study, Cr removal from

an aqueous solution declined from 70 to 14%, when the *Eucalyptus camaldulensis* particle size increased from 0.063 to 2 mm [49], which is consistent with our findings. Higher BET surface area obtained for PWD compared to CWB is another reason for higher adsorption

efficiency and capacity of PWB, as suggested in the literature [50].

Error analysis also indicates high values of SSE for linearized Freundlich isotherm. The SSE values found for the Freundlich model are significantly higher than the obtained values for the Langmuir model. Overally, results indicated no adequate agreement between the predicted and measured adsorption data, implying the lack of validity of the linearized Freundlich isotherm to model the adsorption of the heavy metals onto BC in the leachate. Both linear and non-linear fitting of the experimental data to the Freundlich model yield high R<sup>2</sup> in most cases but the error analysis presented a great difference between linear and non-linear fitting. The value of SSE calculated for non-linear fitting was much lower than that obtained for linear fitting, as it could also be realized by comparing experimental and modeled data presented in Fig. 5d, e and f. Results indicate that nonlinear fitting of the measured data to the Freundlich isotherm could provide significantly more robust prediction compared to the linear fitting. However, the obtained values for the constant n was less than 1 when CWB was used as an adsorbent both for linear and non-linear fitting of data indicating unfavorable adsorption of Pb, Mn, and Cu onto CWB. Results indicated much higher values of  $q_m$  when non-linearized regression was applied. In other words, linearization of the Freundlich isotherm caused underestimation of  $q_m$ , while fitting the measured data to non-linearized form of the Freundlich model depicted greater affinity between the experimental and predicted data. Application of non-linear Freundlich isotherm produced more valid data with significantly higher values of R<sup>2</sup> as well as much smaller SSE. Overally, results indicated that linearization of the Freundlich isotherm to fit the experimental data may generate higher errors and significantly deviate the predicted adsorption capacity of a given adsorbent from the experimental data.

# Temkin isotherm

Temkin isotherm equation contains a factor that reflects the adsorbent-adsorbate interactions. The nonlinear form of Tempkin isotherm is represented by the following equation:

$$q_{\rm e} = \frac{RT}{b_{\rm T}} \ln(K_{\rm T}C_{\rm e}) \tag{13}$$

where, T is the absolute temperature in Kelvin (K), R is the universal gas constant,  $8.314\,\mathrm{J\,mol}^{-1}\,\mathrm{K}^{-1}$ ,  $b_{\mathrm{T}}$  is the constant related to the heat of adsorption indicating the variation of adsorption energy (J mol<sup>-1</sup>), and  $K_{\mathrm{T}}$  is the Temkin equilibrium binding constant (L g<sup>-1</sup>) corresponding to the maximum binding energy. The dimensionless term  $(RT)/b_{\mathrm{T}}$  can be substituted by  $B_{\mathrm{T}}$ , thus Temkin

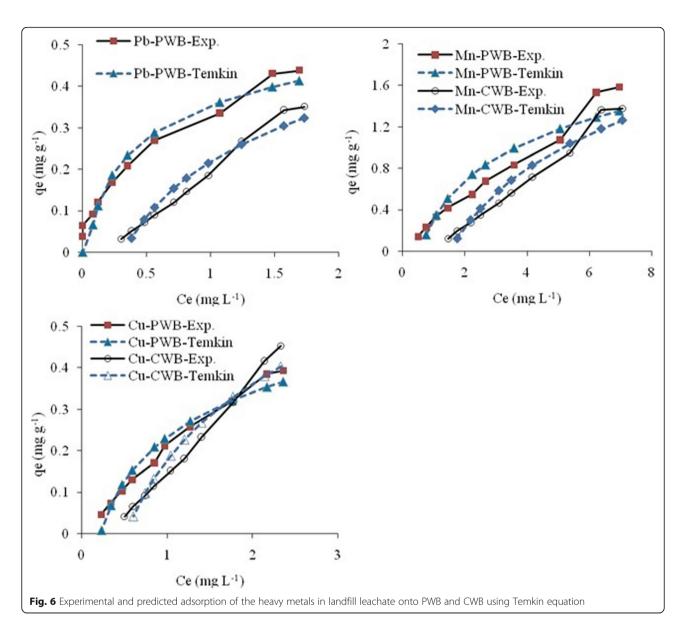
isotherm equation can be linearized as given by the following equation:

$$q_{\rm e} = B_{\rm T} \ln K_{\rm T} + B_{\rm T} \ln C_{\rm e} \tag{14}$$

The obtained parameters of Temkin model are given in Table 5. Values of R<sup>2</sup> found using the linear transformation of the Temkin equation, were comparable to the non-linearized Freundlich model. The variation of adsorption energy,  $b_{\rm T}$ , was positive for all the studied heavy metals implying that the adsorption of Pb, Mn and Cu onto BC is an exothermic reaction (22 kJ mol<sup>-1</sup>). Salam reported that the physical adsorption is characterized by adsorption energy in the range of 5–40 kJ mol<sup>-1</sup> [5]. Physiosorption may occur as a result of weak forces of Van der Waals between the adsorbates and adsorbents [12]. Higher amounts of variation of energy obtained using the Temkin isotherm for adsorption of Pb, Mn, and Cu onto PWB relative to those obtained for CWB indicates greater capacity of PWB to adsorb heavy metals in landfill leachate. It should be noticed that the Temkin isotherm does not provide any estimation of the maximum adsorption capacity of a given adsorbent. In spite of the non-linear Langmuir equation, if the equilibrium concentration is increased, the adsorption capacity of the original Temkin equation,  $q_e$ , does not converge to any limiting value. Figure 6 indicates that the predicted equilibrium curves using Temkin model are very close to those obtained experimentally; however, deviation of the predicted adsorption using the Temkin model slightly increased when lower dosage of BC was applied. Error analysis indicates smaller values of the SSE relative to the Langmuir-1 and linear Freundlich isotherms; however, the non-linear Freundlich model exhibited the lowest values of SSE for adsorption of Pb, Mn and Cu onto BC in this study. Based on the obtained results it seems that Temkin model can adequately describe the adsorption of the heavy metals onto PWB and CWB in the leachate. Adsorption of Pb, Mn and Cu onto BC in landfill leachate was adequately represented by the applied isotherm models, except the linear Freundlich model implying that adsorption of heavy metals onto BC may be controlled by surface diffusion and pore

**Table 5** Temkin isotherm parameters for adsorption of Pb, Mn and Cu onto BC in the leachate

Temkin	Pb		Mn		Cu	Cu		
isotherm parameters	PWB	CWB	PWB	CWB	PWB	CWB		
b <sub>T</sub>	0.11	0.19	0.54	0.82	0.15	0.27		
$K_{T}$	22.3	3.2	1.8	0.7	4.6	2.0		
$R^2$	0.964	0.935	0.889	0.930	0.958	0.938		
SSE	0.004	0.008	0.262	0.131	0.006	0.018		



diffusion simultaneously as well as adsorption at an active preoccupied site. Overally, results indicated promising removal of the heavy metals from landfill leachate using BC, which could be well described by non-linearized Freundlich and Temkin models.

# **Conclusions**

The present study aimed to assess the capability of BC in removal of Pb, Mn and Cu from landfill leachate and model the adsorption kinetics and isotherms of the heavy metals onto BC. Results indicated that the wood-derived BC is an effective adsorbent for the removal of Pb, Mn and Cu from landfill leachate. The adsorption affinity of PWB for Pb, Mn, and Cu was greater than CWB in all treatments. The contact times of 200 and 150 min were sufficient to reach adsorption equilibrium

condition, respectively for PWB and CWB. The removal efficiency of the heavy metals only slightly enhanced as BC dosage exceeded 20 g L<sup>-1</sup>. PWB showed the highest experimental adsorption intensity of 1.58 mg g<sup>-1</sup> for the removal of Mn from the landfill leachate. Beside BC particle size, other properties such as structural and pore space volume of BC may also affect adsorption behavior of heavy metals in aqueous solutions, which is suggested to be further investigated in future studies. The pseudo second-order kinetic model precisely represented the adsorption kinetic data for BC suggesting the chemisorptions of Cd onto BC particles. Calculated  $q_e$  using the Elovich kinetics model also agreed well with the experimental  $q_e$ . Two distinct adsorption stages for the adsorption of the heavy metals onto BC in the leachate was clearly observed; first the migration of metals from the

leachate system to the external surface of BC during which the mass transfer is very rapid and physical processes control the adsorption, followed by the prolonged intra-particle diffusion characterized by slow adsorption. The non-linear Freundlich isotherm best describes the equilibrium adsorption data, followed by the Temkin isotherm. Linearized Freundlich model could only moderately describe adsorption of the heavy metals onto PWB, while it was not able to represent the adsorption by CWB. Linearization method for the Langmuir isotherm also affects the error structure suggesting that the linearization of non-linear isotherm models may violate the theory behind an isotherm and alter error distribution. It is recommended to use wood-derived BC as an effective adsorbent to remove heavy metals from landfill leachate.

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#### Authors' contributions

Ali Daryabeigi Zand (ADZ) was responsible for developing the theory and idea, carrying out the experiments, performing and verifying the analytic calculations and numerical simulations, and writing the manuscript. Maryam Rabiee Abyaneh (MRA) was responsible for carrying out the experiments, performing the analytic calculations and numerical simulations, and writing the manuscript. The authors read and approved the final manuscript.

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#### Availability of data and materials

All data generated or analyzed during this study are included within the article.

#### Competing interests

The authors declare they have no competing interests.

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